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ROUGH WATER PERFORMANCE OF HIGH LENGTH
TO BEAM RATIO PLANING BOATS

# DAVID W. TAYLOR NAVAL SHIP RESEARCH AND DEVELOPMENT CENTER 

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TO BEAM RATIU PLANING BOATS

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|  | d. RECIPIENT'S CATALOO NUMIER |
| 4. TITLE (mid Subritle) <br> ROUGH WATER PERFORMANCE OF HIGH LENGTH TO REAM RA'I'IO PLANING BOATS | 3. TYPE OF REPORT A PEMIOD COVERED |
|  | a. PERTORMING ORG, RETPORT MUMEER |
| 7. AUTHOR(*) <br> E.E. ZARNICK <br> C.R. TURNER <br> 7. PERFORMING CROANIZATION NAME AND ADOREIS David W. Taylor Naval Ship R\&D Center Ship Performance Department Bethesda, MD 20084 |  |
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|  | 10. PROGAMELEMTMT PROJECT, TABK ARIA WORK UNIT Numbens <br> Task Area 2F - 43 - 421001 |
| 11. CONTROLLING OFFICE NAME AND ADDRESS Naval Sea Systems Command Washington, DC 20362 | 12. NEPORT DATE <br> 13. July 1981 <br> 13. NUMDER OF PAGES |
|  | $71$ |
| T4. MONIT SRING AGENCY NAME ADORESS(If dillorent from Controlline Oilice) | 18. SECURITY CLASS. (of thia report)UnclassifiedTBe. OECLASSIFATION/DOWNGRADINGSCHEOLE |
|  |  |
| 16. DISTRIDUTION STATEMENT (OI This Report) <br> Approved for Public Release: Distribution Unlimited |  |
|  |  |  |
| 17. Distribution statement (of tho abetract entored in Block 20, if diftorent tron Raport) |  |
| 16. SUPPLEMENTARY NOTES |  |
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| Planing Boats, Ship Motions, Impact Accelerations |  |
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Waves of the high $\mathrm{I} / \mathrm{t}$ craft. Two problems encountered with the models which may present obstacles in the design of high length to beam ratio craft were the extremely high impact loads as indicated by the high impact accelerations and, large quantities of water over the deck resulting from the bow plowing through wave crests.


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|  | NOTATION |
| :---: | :---: |
| b | Beam of planing boat |
| $\mathrm{C}_{\Delta}$ | Load coefficient, $\Delta / w^{\text {² }}$ |
| d | Rise of center of gravity in smooth water |
| 8 | Acceleration of gravity |
| $\mathrm{H}_{1 / 3}$ | Significant wave height |
| h | Amplitude of CG excursion from mean |
| $\overline{\mathrm{h}}$ | Average value of $h$ |
| ${ }^{\text {h }}$ 1/3 | Average of $1 / 3$ highest $h$ values (significant value) |
| ${ }^{\mathrm{h}} 1 / 10$ | Average of $1 / 10 \mathrm{highest} h$ values |
| $h_{\text {DC }}$ | Mean vertical position of tow doint in waves relative to zero speed floating position in calm water |
| k | Pitch gyradius, in percent of length |
| L | Overall hull length |
| LCG | Longitudinal center of gravity, percent L from stern |
| $\mathrm{R}_{\text {aw }}$ | Added resistance in waves |
| V | Horizontal speed |
| VCG | Vertical center of gravity, height above keel |
| $\mathrm{V} / \sqrt{\mathrm{L}}$ | Speed length ratio, knots/ (ft) 1/2 |
| w | Specific weight of water |
| $\beta$ | Deadrise angle in degrees |
| $\triangle$ | Hull displacement |
| ${ }^{\text {B }}$ Bow | Bow vertical acceleration in gs |
| ${ }^{n} \mathrm{CL}$ | CG vertical acceleration in gs |
| ${ }^{n}$ stern | Stern vertical acceleration in gs |
| 0 | Amplitude of pitch motion in degrees relative to mean |
| $\bar{\theta}$ | Average value of $\theta$ |
| ${ }^{\theta} 1 / 3$ | Average of $1 / 3$ highest $\theta$ values |
| ${ }^{\text {A }} 1 / 10$ | Average of $1 / 10 \mathrm{highest} \theta$ values |
| ${ }^{0} \mathrm{DC}$ | Mean pitch angle in degrecs in maves relative to horizontal |
| $\tau$ | Trim angle of keel in degrees relat: te to horizontal (inc in calm water) |
| ${ }^{T}$ | Static tilm angle |


#### Abstract

abstpact Experiments were conductud in waves with eaveral constant deadrise models to assess the rough water performance of high length to beam ratio planing craft. Several models with $\mathrm{L} / \mathrm{b}=7$ and one with $L / b=9$ were run in wavea to determine the effects on performance of basic design parameters such as speed length ratio, loading coefficient, wave height to beam ratio, deadrise angle, trim angle and length to beam ratio. Charts have been prepared for eatimatiag the pitch and heave motione, vertical accelerations and added resistance in waves of the high $\mathrm{L} / \mathrm{b}$ craft. Two problems encountered with the medels which may present obstacles in the design of high leagth to beam ratio craft were the extremely high impact lixads as indicated by the high impact accelerations and, largs quariti:les of water over the deck resulting from the bow plowing through wave crests.


## ADMINISTRATIVE INFORMATION

The investigation was authorized by the Naval Sea Systems Command and funded under Task Area 2F - 43-421001.

## INTRODUCTION

In anticipation of futurs trends in planing boat design, the data base used in characterizing the rough water performance of planing boats has been extended to include high length to bean ratios. The original data base was provided by Fridsma's ${ }^{l}$ systematic study of constant deadrise prismatic models in irregular waves with length to beam ratios of 4,5 , and 6 . Iice present study has extended this data base to include length to beam ratios of 7 and 9.

Experiments were conducted in waves with several constant deadrise wr ls to determine the effects on performance of several basic design paraneters such as speed length ratio, loading coefficient, wave height to beam ratio, deadrise angle, trim angle and length to beam ratio. Charts were prepared which enable the designer to estimata the pitch, heave, vertical accelerations, and added drag in waves of a high L/b craft.

There did not appear to be any obvious advantages in the rough water performance of high length to beam ratio craft over more conventional length to beam ratios; in fact, the lmpact loads appear to be higher. The models utilized a constant deadrise parabolic bow and it is expected that a more conventional bow would have greatly reduced the slaming problem. Water over the deck, brought about by the models plowing through successive wave crests at high speed, also appeared to be a

Theferences listed on: Page 13
potential problea, This was less of problem on the $L / b=9$ model than on the comparable $\mathrm{L} / \mathrm{b}=7$ model; however, the bow impact accelerations of the $\mathrm{L} / \mathrm{b}=9$ model were higher.

## DESCRIPTION OF MODELS AND INSTRUMENTATION

The models used in these experiments were identical in'frem to those used by Fridsma except for higher $L / b$ ratios. Two models with $L / B=7$ and deadrise angles of 10 and 30 degrees were constructed by the Davidson Laboratory under contract to the Center. The Davidson Laboratory also provided on loan to the Center an existing model with an $L / b=7$ and deadrise angle of 20 degrees. A fourth model was constructed at the Center with an $L / b=9$ and deadrise angle of 20 degrees. All models were fabricated out of aircraft type plywood and high density plastic foam (for the bow shape) to obtain lightweight rigid models appropriate for seaworthiness experiments. A thin plastic strip extending approximately 1 man below the chine was attached to the sidewalls of the models to insure separation during planing. The model lines are shown in Figure 1 and photographs of all fcur models used in the experiments are shown in Figure 2.

The models were towed at constant speed by a lightweight strut consisting of a gimbaled heave staff, that permitted the models freedom in pitch and heave. In order to accommodate the heave staff an aluminum rail was attached to each model which allowed for quick adjustment of the longitudinal position of che tow point and for quick adjustment of ballast weights to obtain the required trim and radius of gyration conditions. The vertical position of the tow point, which corresponded to the pitch axis, was fixed for each model at point 0.39 beams above the keel. The vertical center of gravity varied with loading condition, but was always below the tow point. Table 1 Ifsts the location of the vertical center of gravity (VCG) as a function of loading for all four models. Sirice the ballast weights were moved only along the rail parallel to the baseline, there was no significant change in VCG with trim angle.

Table 1 - VOG* Lecation
VCG/b
MODEL

$$
\begin{gathered}
C_{\Delta}=0.8 \\
0.34 \\
0.36 \\
0.29
\end{gathered}
$$

$B=10^{\circ}, L / B=7$

| $C_{\Delta}=1.0$ | $C_{\Delta}=1.2$ |
| :--- | :---: |
| 0.36 | 0.37 |
| 0.37 | 0.38 |
| 0.32 | 0.33 |
| 0.36 | 0.37 |

$B=30^{\circ}, L / B=7$
0.32
0.37

[^0]The radil of gyration of the unballasted models were determined by auspending each model in air from the pitch gymbal like a pendulum and measuring the period of free oscillations. Calculations of the radius of gyration from the period of free oscillations weremade using the classical equations of a pendulum. The location of the corresponding center of gravity, which is also required for these computations, was obtained by applying a small moment to the suspended model and measuring the resulting static irim angle. The above results were used to compute the location of ballast weights along the model reil for the various experimentel conditions in order to obtain a specified radius of gyration, or conversely, to compute the radius of gyration knowing the location of ballast weights. A radius of gyration equal to 25 percent ship length was originally spectfiad for all conditions, but could not be achieved in the high displacement conditions.

Vertical accelerometers were installed in each model at the bow, stern, and center of gravity. The bow accelerometer was located 10 cm ait of the stem, the $C G$ accelerometer was located above the oitch pivot point and the stern acceleraneter was located 2.5 cm forward of the transom. The gages were force balance type with a range of 50 g and a natural frequency of 1000 Hz (Kistler Model 305A). Special Kistler aignal conditioning equipment was used with the transducer.

Pytch and heave motions of the mociels were measured by potentiometer type transducers mounted on the heave staff or towing strut. A David N. Taylor Naval Shin Research and Development Center (DTNSRDC) designed block gage was also mounted on the strut to measure drag force. Wave height was measured by a sonic probe mounted on the carriage about 20 feet ahead of the model. The models forward of the tow strut were sealed at the deck by a thin sheet of clear plastic to prevent spray and water from entering the models. A lifhtweight movable bren: water also made of clear plastic was mounted on the models near the tow strut. The aft portions of the models were sealed with thin plastic sheet made of "ziploc bags" for quick access to the ballast weights and tow point attachment.

Data were recorded on an Interdaca Model 70 digital computer for on line and off line processing. Vertical accelerations were recorded on analog tape with an Ampex PR 2200 recorder and converted to digital tape, or recorded directly on digital tape for off line processing by the Interdata. The pitch, heave, drag and wave tape height data were sampled at a rate of 75 samples per second after being passed through a 4 pole low pass Butterworth filter with a 15 Hz cutoff. The vertial acceierations were sampled at a rate of 2300 samples per second after being passed through a filter with a 1500 Hz cutoff. A Honeywell Visicorder and a Smborn recorder were used to
visually monitor the data during the experiments.

## EXPERIMENTAL PROGRAM AND PRCCEDURE

The experiments were conducted in irregular waves with sigmificant wave heipht to Leam ratios of $0.222,0.444$, and $0.6 f 6$, and at model spaeds of 4.58 .6 .87 , and 9.16 knota. Typical wave spectra are shown in Figure 3. The above speeds correspond to speed length ratios of 2,3 , and 4 for the models with an $L / b$ ratio of 7 and slightly lower values for the model with an $L / b$ of 9 . Three displacement conditions corresponding to load coefficients of $0.8,1.0$, and 1.2 were examined on all models excluding the model with an $L / b$ ratio of 9 which could not be trimmed properly at a $C_{\Delta}$ of 0.8 . A trim angle of 3 degrees was used throughout the experiments except for the 10 degrees deadrise model which was also tested at trim angles of 2 and 4 derrees and the 30 aegrees deadrise model which was also tested at a trim angle of 2 degrees (both at a load coefficient of 0.8). Early in the test program a judgment was made that running the models at trim angles other than 3 degrees presented an unacceptable risk of severely damaging the models in the high speed sea ctate conditions. On three occasions the model being tested, along with the towing apparatus were severely damaged. Speeds higher than those used in the program could not be run for the same reason, and in several instances, the high speed - sea state condition had to be aborted for the safety of the model and test equipment. Also, the 2 degrees trim angle condition resulted in higher calm water resistance than for either the 3 or 4 dearees trim conditions which were about equal for the 10 degrees deadrise model.

Several calm water runs were made pricr to each : sries of wave runs to obtain the desired operating trim angle for a given speed and loading condition. Ballast weights were moved along the rail in the model to change the location of the longitudinal center of gravity (along with the tow point) until the proper calm water trim angle was obtained. The tow point was always located at the longitudinal center of gravity. This was verified by suspending the model in air by the pitch gymbal or tow point and assuring that the model hung in a balanced or level position. For any CG location, the corresponding location of the ballast weights required to obtain a specific radius of gyration was determined from calculations using information previously obtained for the unballasted model. A radius of gyration of 25 percsat of the ship length was intended for all model experiments, but could not be realized in the light displacement conditions because of insufficient movable ballast weight. In these conditions the models were ballasted to obtain the
specified calm vater trim irreapective of the radius of gyration. Table 2 lists the model configurations that ware used in the experiments including the radius of gyration.

Six passes were made for each condition to obtain approximately 100 amples of mimplitude data to ensure adequate statistical analysis. Most of the data runs (approximately 75 percent) exceeded 100 samples with the highest number being about 300. The remaining data had less than 100 samples per run, with a few as low as 60 samples.

## DATA ANALYSIS

## PITCH ANE HEAVE MOTIONS

In order to characterize the rough water performance of the models, a statistical analysis was performed on the amplitudes or peak values of the motions and accelerations to determine the significant values and other statistical parameters. The procedure followad in the case of the pitch and heave motiors was first to determine the mean values of the time histories for each run and subtract these values from the corresponding data records so that the mean values became the zero reference for the amplitude measurements. The mean value of the pitch motion is the average change in attitude of the keel relative to the horizontal, and the mean value of the heave motion is the average change of the center of gravity in the vertical direction relative to the calm water floating prition at zero speed. The amplitudes were determined by defining a cycle of motion as three consecutive zero crossings, and selecting the largest positive and negative values in the cycle. For the purpose of these experiments, the largest positive value in a cycle was defined as a crest and the largest negative value as a trough. This resulted in pitch bow up and heave down being defined as crests. (Note that this may differ irom other conventions.) The crests and troughs collected from a run were sorted, and computations were made to fetermine various statistical parameters including the significant values and the average of the $1 / 10 \mathrm{highant}$ values. These data are sumarized in Table 3 for the pitch motion and in Table 4 for the heave motion.

The above analysia was performed on the Interdata Model 70 computer which also provided histograms of the data. An attempt was made to fit these histograms to various probability distribution functions. The pitch and heave data (both crests and troughs) for 14 selected runs were fitted to the Rayleigh, Weibull and

Generalized Gatuma distribution functions, and a chi-scrored goodness of fit test performed to determirie the acceptability of each ift. The test was performed at the $\alpha=0.05$ level of significance. A detailed explanation of the tests can be found in most textbooks on statistics (see Reference 2).

Approximately 52 percent of the histograms passed the arceptance test for a Rayleigh distribution and only slightly more ( 55 percent total) passed for a Weibull distribution. The Generalized Camma distribution provided the most acceptance with 71 percent of the histograms passing. Unfortunately, the Generalized Gamma fistribation, which requires three parameters to define, is considerably more complicated to use than the Rayleigh distribution. Using the much simpler Rayleigh distribution to characterize the experimental distribution may, in some instances, lead to errors of about 10 to 15 percent: however, this still may be acceptable for some engineering purposes.

## ACCELERATIONS

The acceleration data were different in character from the motion data and required a slightly different analysis procedure. Time histories of the accelerations from most of these experiments consisted of impact spikes superimposed upon the rigid body accelerations. In spite of the rigid construction of the models, the impact spikes introduced hull vibrations whose frequencies were in the same range as those of the impact spikes. This presented a dilemna in that some of the vibrations could be falsely identified as impact spikes in the processing routine, and filtering the data to remove them would also remove part of the true impact signals. The alternative employed in the analysis involved an interactive graphic display with an individual in the analysis loop selecting each peak. Time histories of the accelerations were projected onto a Tektronix 4015 display terminal, and by aligning a cross hair in close proximity to an impact or peak and pressing an appropriate key, its value was identified and stored by the computer. Figure 4 shows a representative sample time history of acceleration as projected on the Tektronix screen. The small diamonds indicate those values selected for inclusion in the population of peak values. Both rigid body peaks and impact spikes which were measured with reference to the gage zero were included in the population, Accelerations In the direction opposite to the impact spikes were not analyzed. It should be recognized that the impact acceleration measuremencs are influenced to "ome degree $b_{y}$ the hull elasticity and some account of this factor should be given in any design considerations.

The peak acceleration data, after being collected, were analyzed in a similar manner to the motion data and computations made of the significant values and other statistical parameters. These results are presented in Table 5 for bow, midship. and ster-l accelerations.

An attempt was made to fit the acceleration data to the exponential distribution which Fridsma ${ }^{1}$ had found, in his studies. to be a good fit for planing boat accelerations and a chi-squared goodness of fit test was applied to the acceleration data for 14 runs. The exponential distribution was found to be an acceptable fit for approximately 86 percent of the bow data, 67 percent of the stern data, but only for 30 percent of the $C G$ data. It was further found that the exponential distribution provided a good fit to the acceleration data only when the data was composed mainly of impact spikes. This was primarily the case for the bow accelerations where an impact spike occurred nearly every cycle except in the very low speed-sea state conditions. In contrast the CG acceleration data contained a large number of rigid body peaks and this is reflected in the small number of acceptances. This was brought about by the nature of the impact phenomenon and the decision to include both impact spikes and rigid body peaks in the population. The impacts produced a large impulsive angular deceleration which resulted in a stern acceleration spike with opposite sign to that at the bow and a small $\mathcal{O}$ acceleration spike. In many instances the spike at the $C G$ was less than the corresponding rigid body peak. As a consequence, the rigid body accelerations were selected as the peak values in the cycle instead of the impact spikes and became a significant portion of the population. The rigid body accelerations would be expected to follow a distribution more closely resembling those of pitch and heave motions.

## ADDED RESISTANCE IN WAVES

The added resistance in waves was obtained by subtracting the calm water resistance from the corresponding mean cesistance measured in waves. Table 6 presents the added wave resistance obtained by averaging the values from six passes down the basin for each condition. Model resistance data was the most sensitive measurement made and perhaps subject to the most experimental error. An additional complication was experienced with the 20 degrees deadrise model ( $L / B=7$ ). A small strut was attached to the stern of $L . L$ model to measure relative motions during the experiments at loading conditions of $\overbrace{\Delta}=1.0$ and 1.2 . The drag of the strut was larger than
anticipated and may have affected the relationship between trim angle and LCG location while increasing the calm water drag.

## PRESENTATION AND DISCUSSION OF EXPERIMENTAL RESULTS

In order to assist the designer in assessing the rough water performance of a high L/b craft, charts have been prepared for estimating the pitch and heave motions, vertical accelerations and added resistance in waves as a function of significant wave height to beam ratio, loading coefficient, speed length ratio and deadrise angle. A family of faired curves was developed for each set of dato corresponding to a particular deadrise angle and speed length ratio,by fitting the experimental data to a polynomial which was cubic in wave height and quadratic in loading coefficient. In most instances the resulting curves passed exactly through the data spots; however, in some cases minor adjustments had $t$. , be made in order to more accurately reflect the data trend. Each family of faired curves was plotted on a single chart showing the variation of the parameter in question with the significant wave height to beam ratio and loading coefficient. The charts in Figure 5 present the significant values of pitch crests and troughs for the 10 -degree deadrise model at a trim angle of 3 degrees and speed length ratios of 2,3 , and 4. Similar results are shown in Figure 6 for heave crests and troughs. Significant values of vertical acceleration (impact side only) for the same model are presented in Figure 7 and the added drag is presented in Figure 8. A corresponding set of data are presented in Figures 9 through 12 for the 20 degree deadrise angle model with $L / b=7$ and in Figures 13 through 16 for the 30 degrec deadrise model.

These charts can be used directly for interpolaing results for any value of wave height to beam ratio between 0.2 and 0.7 and loading coefficient, $C_{\Delta}$, from 0.8 to 1.2 at speed length ratios of 2,3 , or 4 and deadrise angles of 10,20 or 30 degrees. A linear interpolation can be used for any value of speed length ratio or deadrise angle between those contained on the charts and the interpolation can be applied sequeritially.

Since there was only a small amount of experimental deta obtained at trim angles other than 3 degrees, no generalized method was developed for extropolating the results on the charts to other operating trim angles. Also, no means have been derived for the extrapolating the results to higher length to beam ratios, but a higher length to
beam ratio was examined in experiments using a 20 -degree deadrise model with a length to beam ratio of 9 . Although the gross trends were clearly demonstrater, the data were not considered sufficient to determine the precise variations with length beam ratio in the general case.

The charts not only provide a means of assessing the rough water performance of high $\mathrm{L} / \mathrm{b}$ craft, but also show the effects of changes in basic hull parameters on this performance. Some of the broad trends in performance can be readily deduced from the charts and this has been incorporated into the discussion below along with other general observations and information not concained in the charts.

The three speed length ratios used in these experiments were selected to cover the broadest possible range of cperation of high $\mathrm{L} / \mathrm{b}$ planing craft. At $\frac{V}{\sqrt{L}}=2$, the craft essentially operated in the displacement mode. at $\frac{V}{\sqrt{L}}=3$, separation occurred along the chine with some side wetting near the stern and at $\frac{V}{\sqrt{L}}=4$, separation occurred along the entire chine. In all cases, there was a clean break away of water behind the transom. At the higher speeds, a large portion of the bow rode out of the water except when pitching downward, during which time, a slam or water impact usually occurred.

The pitch motion decreased with increased speed while the added resistance in waves increased. There was no similar clear cut trend in heave, although it tended to be less at high speed in most cases. Bow acceleration did nut show any consistent trend with speed and appeared to be a cumpiex function of both speed and deadrise angle.

At high speed in high waves, there were a few occasions when the entire keel of the $\mathrm{L} / \mathrm{b}=7$ models became completely unwetted while transiting between consecutive crests. A more serious problem encountered in these conditions was that of heavy spray and water spilling over the deck. This problem was sensitive to both trim angle and ioading conditions as well as the speed.

Only a small number of experiments were comaticted at trim angles other tha: 3 degrees; nevertheless, some insight into the gross effects of trim angle on performance can be deduced from these results. At a trim angle of 2 degrees, which was run with 10 -and 30 -degree deadrise models at $C_{\Delta}=0.8$, the motion and vertical accelerations were substantially less than those obtained at a trim angle of 3 degrees. At 4 degrees of trim angle, which was run with the 10 -degree deadrise model, the motions and accelerations in general were larger than those at 3 degrees of trim angle. Calm water resistance was highest at 2 degrees of trim angle. However, the
corresponding added resistance in waves was about the same as for the 3 degrees of trim angle, except at $\frac{V}{\sqrt{L}}=4$ in the high sea condition, where the 10 -degrees deadrise model showed arge increase. There was no significant difference in the calm water resistance or added resistance in waves between the 3 degrees and 4 degrees of trim angle conditions.

Although the motions and accelerations were less at the 2 degrees of trim angle condition, the accompanying deck wetness problems were considered too severe at some of the high speed-sea state conditions for it to be a practizal operating condition. At high speed, the bow of the $L / b=$ ? models tended to plunge or crash through consecutive wave crests, with large amounts of water spilling over the top of the deck. In the high sea condition at $\frac{V}{\sqrt{L}}=4$, the 10 -degree deadrise model was torn off the tow strut by the force of the water spilling over the deck. Experiments with the 30 degree deadrise model at 2 degrees of trim showed similar tendencies and experiments in the high sea condition could not be run either at $\frac{V}{\sqrt{L}}=3$ or 4 because of the high risk of severely damaging the model and test appartatus. This was a major consideration in Iimiting the experiments to trim angles of 3 degrees where this problem did not appear to be quite as severe except at high loading conditions ( $C_{\Delta}=1.2$ ); here again experiments could not be conducted at the high speed condition in high, waves. because of this problem a portion of the charts shown in the figures for $\bar{J} \bar{L}=4$ could not be completed. This region is indicated by a broken line on the charts and is defined as a bow wetness limic.

As might have been expected, the deadrise angle had the most proncunced effect upon the impact accelerations. The bow acceleration for the 10 -degree deadrise model was more than twice that of the 30 sumewhere in between the two extremes. There were differences in the motions and added drag in waves, but they do not appear to be significant.

Experiments were conducted with an $L / b=9$ model with 20 -degree deadrise angle to establish an upper bound on the effects of increasing length to beam ratio. The results showed that although the differences in the motions were not large, the vertical accelerations for the $L / b=9$ model were almost twice as high as for the $L / b=7$ model at the same speed. The is probably the result of a higiner water entry velocity at the bow of the $L / b=9$ model because of its extra length. The added resistance in waves was less for the $L / b=9$ model at the higher speeds and abuut the same at low speed. It was also noted that bow wetness was less with the higher $L / b$ rat 10 and that experiments could be safely conducted at high speed in the heavy loading condition.

## SUMMARY AND CONCLUSIONS

Experiments were conducted in waves with several constant deadrise models to assess the rough water performance of high length to beam ratio planing craft. Several models with $L / b=7$ and one with $L / b=9$ were run in waves to determine the effects on performance of basic design parameters such as speed length ratio, loading coefficient, wave height to beam ratio, deadrise angle, trim angle and length to beam ratio. Charts have been prepared for estimating the pitch and heave motions, vertical accelerations and added resistance in waves of high $L / b$ craft.

Two problems encountered with the models widch may present obstacles in the design of high length to beam ratio craft were the extremely high impact loads as indicated by the high impact accelerations, and large quantities of water over the deck resulting from the bow plowing through wave crests. Qperating at trim angles necessary for planing resulted in a portion of the bow riding out of the water which was highly conducive to bow slamming. Also, increasing length to beam ratio for a given beam increased the vertical velocity at the bow because of the corresponding increase in the pitch lever aim. By employing a conventional bow in place of the constant deadrise parabolic bow used on the models, some reduction in the impact loading may be realized by achieving a smoother water entry.

At high speed, conditions existed where che model plowed through wave crests spilling large amounts of water over the deck. This occurred at a low trim angle ( $\tau=2^{\circ}$ ) for the lightly loaded conditicns ( $C_{\Delta}=0.8$ ) and at a moderate trim angle ( $\tau=3^{\circ}$ ) for the heavily loaded conditions ( $C_{\Delta}=1.2$ ). These occurrences proved to be disastrous to the model on several occasions. The deck wetness and wave plow-in were somewhat less on the $L / b=9$ model; however, as indicated previously, the bow impact accelerations increased. The full-scale vehicle with a more conventional bow and increased freeboard may be better al ? to recover from such events and, more than likely, would never be operated at such extreme conditions; nevertheless, water over the bow is atill a major factor to be opisidered in any design.

The advantages of the high length to beam ratio craft (from a hydrodynamic point of view) may lie primarily in its resistance characteristics. There does not appear to be any obvious advantages in its overall rough water performance over that of moderate length to beam ratio craft, in fact the impact acceleration and loads appear to be higher. Nevertheless, there may be special applications for which high length to beam planing craft are preferable to conventional length to beam ratio or displacement type craft.

ACKNOWLEDGMENTS
Acknowledgment is given to Mr. Brooks Peters for the development of all data analysis routines and procedures and to Mr. Martin Dipper who helped implement them.

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TABLE 2

## MODEL CONF IGURATIONS

| Symbol | L/b | $\beta$ | $c_{\Delta}$ | LCG | $\tau$ | k | v/r | d/b | $\tau_{0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| A | 7 | 10 | 0.8 | 65.5 | 3.0 | 28.0 | 2.00 | -. $011^{\text {* }}$ | ---- |
| B | " | 11 | 1 | 65.1 | 1 | 27.0 | 3.00 | . 014 | -..-- |
| C | " | " | 11 | 62.5 | " | 26.0 | 4.00 | . 056 | . 10 |
| D | " | " | 1.0 | 60.7 | " | 25.4 | 2.00 | -. 021 | 41 |
| E | 1 | 11 | 1 | 59.0 | " | 25.3 | 3.00 | . 013 | 1.40 |
| F | " | 1 | " | 58.5 | " | 25.3 | 4.00 | . 035 | 0.97 |
| $G$ | " | " | 1.2 | 59.5 | " | 23.8 | 2.00 | -. 020 | 1.34 |
| H | " | " | 11 | 58.5 | 1 | 24.3 | 3.00 | . 015 | 1.12 |
| 1 | " | 1 | " | 56.7 | 1 | 24.1 | 4.00 | . 041 | 0.72 |
| $J$ | " | 11 | 0.8 | 59.4 | 2.0 | 24.0 | 2.00 | -. 011 | 0.70 |
| K | " | 11 | 11 | 57.5 | " | 24.0 | 3.00 | . 010 | 0.49 |
| L | 11 | 1 | " | 56.3 | 11 | 23.0 | 4.00 | . 032 | 0.28 |
| M | " | 11 | 1 | 69.0 | 4.0 | 30.0 | 2.00 | -. 008 | 2.13 |
| $N$ | " | " | " | 67.1 | 1 | 29.0 | 3.00 | . 032 | 1.80 |
| 0 | " | 11 | " | 64.7 | 1 | 27.0 | 4.00 | . 069 | 1.50 |
| $P$ | 11 | 20 | " | 64.4 | 3.0 | 25.3 | 2.00 | -. 015 | 1.53 |
| Q | " | 1 | " | 64.4 | 11 | 25.3 | 3.00 | . 016 | 1.53 |
| R | ' | " | 1 | 64.4 | " | 25.3 | 4.00 | . 036 | 1.30 |
| S | 11 | 1 | 1.0 | 61.4 | " | 25.3 | 2.00 | . 001 | 1.43 |
| T | " | ${ }^{\prime \prime}$ | 11 | 61.1 | " | 24.9 | 3.00 | . 001 | 1.36 |
| U | " | 1 | 11 | 59.1 | " | 24.3 | 4.00 | . 001 | 1.06 |
| $v$ | 7 | 20 | 1.2 | 59.4 | 3.0 | 24.3 | 2.00 | . 001 | 1.30 |
| W | 11 | " | 1 | 58.3 | 1 | 25.1 | 3.00 | . 003 | 1.12 |
| $x$ | " | " | " | 56.7 | 11 | 25.0 | 4.00 | . 001 | 0.91 |
| Y | 9 | " | 1.0 | 61.9 | 11 | 24.8 | 1.56 | . 002 | 1.95 |
| 2 | " | " | " | 59.3 | 11 | 24.6 | 2.33 | . 004 | 1.86 |
| AA | " | " | 1 | 60.0 | 11 | 24.4 | 3.11 | . 003 | 1.75 |
| 8 B | " | " | 1.2 | 67.9 | " | 23.7 | 1.56 | -. 020 | ---- |
| CC | 11 | 11 | 11 | 67.6 | ${ }^{\prime \prime}$ | 23.8 | 2.37 | -. 009 | 1.82 |

[^1]TABLE 2
mOdel CONFigurations (COntinued)

| Symbol | L/b | $\beta$ | $c_{\Delta}$ | LCG | $\tau$ | k | v/L | d/b | ${ }_{0}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| DD | 9 | 20 | :. 2 | 67.1 | 3.0 | 24.2 | 3.11 | . 034 | 1.76 |
| EE | 7 | 30 | 0.8 | 60.6 | $\cdots$ | 24.0 | 2.00 | -. 013 | 1.90 |
| FF | " | 1 | 11 | 59.9 | " | 24.0 | 3.00 | -. 007 | , 45 |
| GG | " | 1 | " | 58.7 | " | 23.0 | 4.00 | 7 | . 60 |
| : H | " | " | 1.0 | 62.7 | " | 25.3 | 2.00 | -. 016 | . 60 |
| 11 | " | " | 1 | 62.2 | " | 25.4 | 3.00 |  | . 60 |
| JJ | " | " | 11 | 61.2 | " |  |  | . 010 | . 53 |
| KK | " | 1 | 1.2 | 3 | " |  |  | . 030 | 1.34 |
| LL | : | " | 11 |  |  |  | 2.00 | -. 020 | 1.30 |
| MM | " | " | " |  |  | 25.0 | 3.00 | . 011 | 1.30 |
| NN | 11 | 11 |  | 58.7 | " | 26.0 | 4.00 | . 031 | 0.98 |
| N | " | " | 0.8 | 65.9 | 2.0 | 28.0 | 2.00 | -. 012 | 1.00 |
| 00 | " | " | " | 64.7 | " | 27.0 | 3.00 | . 003 | 0.88 |
| PP | 1 | " | " | 64.2 | " | 27.0 | 4.00 | . 018 | 0.70 |

table 3
PITCH MOTIONS

|  |  |  |  | CREST |  |  | TROUGH |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Condition | $\begin{aligned} & \text { Contigu- } \\ & \text { ration } \end{aligned}$ | $\mathrm{H}_{1 / 3} / \mathrm{b}$ | ${ }^{\theta} \mathrm{dc}$ | $\bar{\theta}$ | ${ }^{0} 1 / 3$ | ${ }_{1} / 10$ | $\bar{\theta}$ | ${ }^{1} /{ }^{3}$ | $\theta_{1 / 10}$ |
| 1 | A | . 260 | 3.32 | 1.22 | 2.18 | 3.08 | 1.27 | 2.08 | 2.82 |
| 2 | A | . 417 | 3.07 | 2.26 | 3.91 | 5.37 | 2.38 | 3.80 | 5.27 |
| 3 | A | . 664 | 3.23 | 3.49 | 5.59 | 6.90 | 3.80 | 5.63 | 6.59 |
| 4 | B | . 261 | 3.44 | 0.99 | 1.83 | 2.49 | 1.16 | 1.98 | 2.76 |
| 5 | B | . 409 | 3.64 | 1.91 | 3.22 | 4.15 | 2.29 | 3.70 | 4.70 |
| 6 | B | . 647 | 3.77 | 2.88 | 4.51 | 4.94 | 3.47 | 5.70 | 6.82 |
| 7 | C | . 275 | 3.05 | 0.82 | 1.35 | 1.66 | 1.08 | 1.57 | 1.86 |
| 8 | C | . 436 | 3.22 | 1.73 | 2.72 | 3.13 | 2.13 | 3.54 | 4.43 |
| 9 | c | . 647 | 3.36 | 2.42 | 3.71 | 4.49 | 3.17 | 5.06 | 6.18 |
| 10 | 0 | . 227 | 3.03 | 1.48 | 2.38 | 3.09 | 1.50 | 2.36 | 3.02 |
| 11 | D | . 475 | 3.24 | 2.99 | 5.10 | 7.08 | 3.17 | 5.01 | 6.58 |
| 12 | 0 | . 684 | 3.47 | 3.68 | 6.13 | 7.79 | 3.97 | 6.36 | 7.79 |
| 13 | E | . 311 | 2.67 | 1.26 | 1.95 | 2.40 | 1.51 | 2.66 | 3.47 |
| 14 | E | . 503 | 2.72 | 2.03 | 3.10 | 3.84 | 2.53 | 4.17 | 5.22 |
| 15 | E | . 684 | 2.87 | 2.46 | 3.89 | 4.62 | 3.19 | 5.27 | 6.48 |
| 16 | F | . 235 | 3.00 | 0.92 | 1.39 | 1.59 | 1.21 | 1.88 | 2.20 |
| 17 | F | . 424 | 2.78 | 1.52 | 2.36 | 2.12 | 1.84 | 1.46 | 4.17 |
| 18 | $F$ | . 617 | 2.12 | 1.81 | 3.19 | 4.19 | 2.48 | 4.09 | 5.20 |
| 19 | $G$ | . 270 | 2.91 | 1.01 | 1.64 | 1.98 | 0.93 | 1.51 | 2.02 |
| 20 | $G$ | . 368 | 2.98 | 1.76 | 2.80 | 3.37 | 1.82 | 2.77 | 3.15 |
| 21 | G | . 592 | 3.07 | 2.90 | 4.76 | 6.10 | 2.93 | 4.89 | 4.98 |
| 22 | H | . 228 | 2.92 | 0.63 | 1.03 | 1.19 | 0.70 | 1.19 | 1.52 |
| 23 | H | . 463 | 2.97 | 1.83 | 3.01 | 3.91 | 2.18 | 4.06 | 6.18 |
| 24 | H | . 596 | 2.73 | 2.39 | 3.81 | 4.82 | 2.78 | 4.66 | 6.14 |
| 25 | 1 | . 248 | 2.99 | 0.69 | 1.12 | 1.42 | 0.77 | 1.28 | 1.47 |
| 26 | 1 | . 389 | 2.87 | 1.20 | 1.83 | 2.24 | 1.46 | 2.44 | 3.05 |
| 27 | 1 | ---- | ---- | ---- | ---- | ---- | ---- | ---- |  |
| 28 | J | . 297 | 2.00 | . 942 | 1.55 | 2.14 | 0.94 | 1.56 | 2.16 |
| 29 | J | . 443 | 2.07 | 2.01 | 3.27 | 4.04 | 2.01 | 3.12 | 3.85 |

TABLE 3
PITCH MOTIONS (CONTINUED)

|  |  |  |  | CREST |  |  | TROUGH |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Condition | Conf. | $H_{i / 3 / b}^{b}$ | ${ }^{\theta} \mathrm{dc}$ | $\bar{\theta}$ | ${ }^{9} 1 / 3$ | $0^{1 / 20}$ | $\dot{\bar{\theta}}$ | 61/3 | ${ }^{\theta} 1 / 10$ |
| 30 | $J$ | . 734 | 2.22 | 3.53 | 5.53 | 6.93 | 3.56 | 5.54 | 6.75 |
| 31 | k | . 229 | 1.93 | 0.45 | 0.79 | 0.99 | 0.51 | 0.90 | 1.24 |
| 32 | $k$ | . 444 | 1.76 | 1.34 | 2.06 | 2.39 | 1.60 | 2.78 | 3.80 |
| 33 | $k$ | . 694 | 1.75 | 2.57 | 3.86 | 5.08 | 2.96 | 4.59 | 5.38 |
| 34 | L | . 248 | 1.99 | 0.55 | 0.92 | 1.10 | 0.66 | 1.09 | 1.36 |
| 35 | L | . 392 | 1.91 | 1.18 | 1.99 | 2.50 | 1.38 | 2.36 | 3.00 |
| 36 | L | . 750 | 1.83 | 2.29 | 3.45 | 4.00 | 3.63 | 5.68 | 7.12 |
| 37 | M | . 267 | 4.47 | 1.26 | 2.44 | 3.65 | 1.25 | 2.16 | 2.88 |
| 38 | M | . 424 | 5.39 | 2.66 | 4.62 | 6.10 | 2.82 | 4.27 | 5.53 |
| 39 | M | . 714 | 5.04 | 4.31 | 7.15 | 8.96 | 4.46 | 6.47 | 7.68 |
| 40 | $N$ | . 284 | 4.16 | 1.02 | 1.73 | 2.18 | 1.15 | 1.72 | 2.11 |
| 41 | $N$ | . 464 | 4.40 | 2.45 | 4.14 | 5.45 | 2.92 | 4.54 | 5.38 |
| 42 | $N$ | . 617 | 4.51 | 2.89 | 4.76 | 5.73 | 3.48 | 5.44 | 6.46 |
| 43 | 0 | . 298 | 3.89 | 1.00 | 1.71 | 2.08 | 1.25 | 1.87 | 2.29 |
| 44 | 0 | . 454 | 4.08 | 2.12 | 3.28 | 3.98 | 2.58 | 3.82 | 4.29 |
| 45 | 0 | ---- | ---- | --.. | --.- | ---- | ---- | ---- | ---- |
| 46 | P | . 226 | 3.01 | 0.93 | 1.59 | 2.11 | 0.56 | 1.50 | 1.95 |
| 47 | P | . 399 | 3.23 | 2.16 | 3.72 | 5.05 | 2.31 | 3.76 | 4.89 |
| 48 | $P$ | . 705 | 3.38 | 3.47 | 5.82 | 7.39 | 3.73 | 5.90 | 7.25 |
| 49 | Q | . 238 | 3.14 | 0.79 | 1.28 | 1.58 | 0.88 | 1.39 | 1.79 |
| 50 | Q | . 355 | 3.02 | 1.55 | 2.63 | 3.40 | 1.84 | 2.95 | 3.89 |
| 51 | Q | . 620 | 3.38 | 2.76 | 4.53 | 5.31 | 3.44 | 5.25 | 6.28 |
| 52 | R | . 221 | 3.04 | 0.71 | 1.16 | 1.47 | 0.81 | 1.31 | 1.62 |
| 53 | R | . 401 | 3.16 | 1.52 | 2.45 | 2.96 | 1.94 | 2.98 | 3.79 |
| 54 | R | . 602 | 3.21 | 2.24 | 3.71 | 4.46 | 2.99 | 4.59 | 5.44 |
| 55 | S | . 321 | 3.00 | 1.90 | 3.25 | 4.23 | 1.97 | 3.07 | 3.87 |
| 56 | s | . 390 | 3.27 | 2.65 | 4.46 | 5.82 | 2.76 | 4.25 | 5.16 |
| 57 | S | . 659 | 3.48 | 3.58 | 5.95 | 6.66 | 3.94 | 6.16 | 7.74 |
| 58 | T | . 289 | 2.92 | 1.40 | 2.03 | 2.22 | 1.65 | 2.56 | 3.22 |

TABLE 3
PITCH MOTIONS (CONTINUED)

| Condition | Conf. | $H_{1 / 3 / b}$ | ${ }^{\theta} \mathrm{dc}$ | CREST |  |  | trough |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\bar{\theta}$ | ${ }^{0} 1 / 3$ | ${ }^{0} 1 / 10$ | $\overline{0}$ | ${ }^{8} 1 / 3$ | ${ }^{\theta} 1 / 10$ |
| 58 | T | . 414 | 3.04 | 1.84 | 2.91 | 3.57 | 2.32 | 3.76 | 4.71 |
| 60 | T | . 675 | 3.36 | 2.61 | 4.18 | 5.08 | 3.21 | 5.00 | 6.05 |
| 61 | $u$ | . 332 | 2.46 | 1.07 | 1.60 | 1.83 | 1.30 | 2.18 | 2.74 |
| 62 | U | . 483 | 2.50 | 1.66 | 2.38 | 2.69 | 2.04 | 3.18 | 3.91 |
| 63 | $u$ | . 602 | 2.32 | 1.86 | 2.98 | 3.65 | 2.36 | 4.05 | 5.26 |
| 64 | $v$ | . 295 | 2.94 | 1.81 | 2.89 | 3.76 | 1.81 | 2.81 | 3.58 |
| 65 | $v$ | . 485 | 3.19 | 3.02 | 5.02 | 6.36 | 3.14 | 4.93 | 6.13 |
| 66 | $v$ | . 688 | 3.50 | 3.76 | 5.91 | 6.62 | 4.03 | 5.96 | 6.81 |
| 67 | W | . 275 | 2.81 | 1.14 | 1.64 | 1.98 | 1.28 | 2.04 | 2.75 |
| 68 | W | . 479 | 3.15 | 2.09 | 3.06 | 3.69 | 2.42 | 3.85 | 4.82 |
| 69 | W | . 636 | 2.94 | 2.46 | 3.71 | 4.44 | 3.01 | 4.71 | 5.77 |
| 70 | $x$ | . 228 | 2.71 | 0.83 | 1.43 | 1.77 | 0.92 | 1.45 | 1.68 |
| 71 | $x$ | ---- | ---- | ---- | ---- | ---- | -..-- | .-.-- | ...-- |
| 72 | $x$ | ---- | ---- | ---- | ---- | ---- | ---- | ---- | ---- |
| 73 | $x$ | . 278 | 3.49 | 1.69 | 2.81 | 3.67 | 1.68 | 2.33 | 2.73 |
| 74 | $\gamma$ | . 460 | 3.89 | 2.62 | 4.69 | 5.89 | 2.74 | 3.91 | 4.86 |
| 75 | $Y$ | . 647 | 3.89 | 3.39 | 5.42 | 5.91 | 3.82 | 5.17 | 6.05 |
| 76 | $z$ | . 298 | 3.50 | 1.39 | 2.32 | 2.83 | 1.56 | 2.09 | 2.30 |
| 77 | 2 | . 551 | 3.94 | 2.28 | 3.87 | 5.11 | 2.69 | 3.56 | 3.92 |
| 78 | 2 | . 675 | 4.16 | 2.69 | 4.38 | 5.22 | 3.11 | 4.49 | 5.06 |
| 79 | AA | . 258 | 3.29 | 1.01 | 1.65 | 2.09 | 1.21 | 1.67 | 2.04 |
| 80 | AA | . 487 | 3.55 | 1.55 | 2.60 | 3.17 | 1.80 | 2.68 | 3.35 |
| 81 | AA | . 666 | 3.74 | 2.33 | 3.89 | 4.78 | 2.73 | 4.05 | 4.78 |
| 82 | BB | . 216 | 3.16 | 0.72 | 1.23 | 1.60 | 0.67 | 1.10 | 1.42 |
| 83 | BB | . 487 | 3.60 | 2.81 | 4.71 | 5.98 | 2.87 | 4.19 | 4.81 |
| 84 | B8 | . 634 | 3.72 | 3.31 | 5.56 | 6.98 | 3.39 | 5.09 | 6.14 |
| 85 | CC | . 259 | 3.18 | 0.83 | 1.42 | 1.91 | 0.86 | 1.31 | 1.59 |
| 86 | CC | . 401 | 3.43 | 1.70 | 2.82 | 3.79 | 1.87 | 2.75 | 3.26 |
| 87 | CC | . 685 | 3.66 | 2.89 | 4.92 | 6.19 | 3.30 | 4.90 | 5.84 |

TABLE 3
PITCH MOTIONS (CONTINUEO)

| Condition | Conf. | $H_{1} / 3 / b$ | ${ }^{\theta} \mathrm{dc}$ | CREST |  |  | TROUGH |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\bar{\theta}$ | $\theta_{1 / 3}$ | $\theta_{1 / 10}$ | $\overline{0}$ | ${ }^{0} 1 / 3$ | ${ }^{6} 1 / 10$ |
| 88 | DD | . 222 | 3.21 | 0.56 | 0.96 | 1.30 | 0.58 | 0.95 | 1.19 |
| 89 | DD | . 401 | 3.62 | 1.78 | 2.97 | 3.41 | 2.18 | 3.44 | 3.90 |
| 90 | 00 | . 614 | 3.65 | 2.40 | 3.97 | 5.20 | 3.02 | 4.53 | 5.54 |
| 91 | EE | . 269 | 3.31 | 1.29 | 2.21 | 2.64 | 1.28 | 2.00 | 2.45 |
| 92 | EE | . 462 | 3.73 | 2.72 | 4.78 | 6.36 | 2.84 | 4.36 | 5.50 |
| 93 | EE | . 632 | 3.75 | 3.61 | 6.05 | 7.46 | 3.53 | 5.57 | 6.81 |
| 94 | FF | . 223 | 3.03 | 0.91 | 1.56 | 1.94 | 0.98 | 1.55 | 1.93 |
| 95 | FF | . 365 | 3.07 | 1.45 | 2.66 | 3.65 | 1.61 | 2.95 | 4.01 |
| 96 | FF | . 620 | 3.35 | 2.91 | 4.76 | 5.78 | 3.32 | 5.23 | f. 57 |
| 97 | GG | . 218 | 3.22 | 0.69 | 1.20 | 1.63 | 0.77 | 1.23 | 1.56 |
| 98 | GG | . 355 | 3.39 | 1.29 | 2.15 | 2.53 | 1.56 | 2.66 | 3.40 |
| 99 | GG | . 621 | 3.46 | 2.38 | 3.68 | 4.93 | 3.13 | 4.63 | 5.46 |
| 100 | HH | . 247 | 3.17 | 1.83 | 2.94 | 3.75 | 1.83 | 2.74 | 3.14 |
| 101 | HH | . 503 | 2.49 | 3.30 | 5.52 | 6.86 | 3.49 | 5.37 | 6.41 |
| 102 | HH | . 616 | 3.56 | 3.37 | 5.74 | 7.36 | 3.55 | 5.49 | 0.87 |
| 103 | 11 | . 225 | 3.01 | 1.30 | 2.01 | 2.44 | 1.45 | 2.24 | 2.78 |
| 104 | 11 | . 453 | 3.24 | 2.17 | 3.34 | 3.82 | 2.63 | 4.00 | 4.32 |
| 105 | 11 | . 748 | 3.71 | 2.99 | 4.60 | 5.23 | 3.62 | 5.55 | 6.29 |
| 106 | JJ | . 288 | 3.02 | 1.03 | 1.66 | 2.00 | 1.25 | 1.94 | 2.29 |
| 107 | JJ | . 478 | 3.00 | 1.69 | 2.56 | 2.98 | 2.22 | 3.41 | 4.14 |
| 108 | JJ | . 694 | 3.22 | 2.29 | 3.55 | 4.29 | 2.88 | 4.63 | 5.76 |
| 109 | KK | . 219 | 2.96 | 0.96 | 1.55 | 1.98 | 0.97 | 1.58 | 2.00 |
| 110 | KK | . 362 | 3.00 | 1.88 | 3.25 | 4.49 | 1.92 | 3.21 | 4.33 |
| 111 | KK | . 634 | 3.05 | 3.22 | 5.60 | 7.22 | 3.30 | 5.35 | 6.40 |
| 112 | LL | . 219 | 3.03 | 0.59 | 1.00 | 1.38 | 0.64 | 1.07 | 1.48 |
| 113 | LL | . 380 | 2.87 | 1.58 | 2.62 | 3.62 | 1.67 | 2.92 | 3.93 |
| 114 | LL. | . 587 | 3.24 | 2.67 | 4.30 | 5.07 | 3.08 | 4.99 | 6.06 |
| 115 | MM | . 228 | 2.92 | 0.55 | 0.88 | 0.96 | 0.60 | 1.02 | 1.39 |
| 116 | MM | . 330 | 2.91 | 1.19 | 1.79 | 2.12 | 1.39 | 2.18 | 2.70 |

table 3
PITCH MOTIONS (CONTINUED)

| Condition | Conf. | $\mathrm{H}_{1} /{ }^{3} \mathrm{~b}$ | $\theta_{\text {dc }}$ | CREST |  |  | TROUGH |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $\vec{\theta}$ | ${ }^{1} 1 / 3$ | ${ }^{\theta} /{ }_{2} 0$ | $\bar{\theta}$ | ${ }^{1} 1 / 3$ | $\theta_{1 / 10}$ |
| 117 | MM | ---- | ---- |  |  |  |  |  |  |
| 118 | NN | . 215 | 2.18 | 1.02 | 1.64 | 1.99 |  |  |  |
| 119 | NN | . 351 | 2.33 | 1.77 | 3.15 | 4.43 |  | 0 | 93 |
| 120 | NN | . 698 | 2.46 | 3.37 |  | 7. | 51 | 2.90 | , |
| 121 | 00 | . 236 | 2.00 | . 80 | 1.30 |  | . 51 | 5.78 | 7.25 |
| 122 | 00 | . 420 | 2.13 |  | 1.3 | 1.71 | 0.90 | 1.46 | 1.89 |
|  |  | . 420 | 2.13 | 1.65 | 2.72 | 3.52 | 1.99 | 3.45 | 5.15 |
| 123 | 00 | . 634 | 2.01 | 2.61 | 4.04 | 4.82 | 3.11 | 4.86 | 5.88 |
| 124 | PP | . 225 | 1.99 | 0.56 | 0.95 | 1.19 | 0.67 | 1.07 | 1.42 |
| 125 | PP | ---- | ---- | - | -.--- |  |  |  | . 42 |
| 126 | PP | ---- | ---- |  |  |  |  |  |  |

TABLE 4
heave motions

| Condition | Configuration | $H_{1 / 3 / b}$ | $h_{\mathrm{dc} / \mathrm{b}}$ | CREST |  |  | TROLGH |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $h / b$ | $\mathrm{h}_{1 / 3} / \mathrm{b}$ | $\mathrm{h}_{1 / 10 / b}$ | $\mathrm{h} / \mathrm{b}$ | ${ }^{4} 1 / 3 / b$ | $h_{1 / 10 / b}$ |
| 1 | A | . 260 | -. 003 | . 035 | . 064 | . 088 | . $04!$ | . 080 | . 121 |
| 2 | A | . 417 | -. 002 | . 089 | . 156 | . 231 | . 100 | . 185 | . 286 |
| 3 | A | . 664 | -. 014 | . 178 | . 290 | . 359 | . 206 | . 340 | . 441 |
| 4 | B | . 261 | . 038 | . 036 | . 061 | . 084 | . 042 | . 080 | . 120 |
| 5 | B | . 409 | . 045 | . 090 | . 152 | . 194 | . 113 | . 198 | . 265 |
| 6 | B | . 647 | . 039 | . 197 | . 330 | . 383 | . 238 | . 391 | . 462 |
| 7 | C | . 275 | . 064 | . 033 | . 052 | . 062 | . 039 | . 066 | . 082 |
| 8 | C | . 436 | . 071 | . 100 | . 166 | . 213 | . 111 | . 191 | . 256 |
| 9 | C | . 647 | . 063 | . 179 | . 295 | . 342 | . 204 | . 335 | . 423 |
| 10 | D | . 227 | -. 020 | . 043 | . 072 | . 095 | . 049 | . 082 | . 114 |
| 11 | D | . 475 | -. 013 | . 112 | . 187 | . 241 | . 126 | . 236 | . 337 |
| 12 | D | . 684 | -. 009 | . 183 | . 305 | . 389 | . 209 | . 359 | . 470 |
| 13 | E | . 311 | . 009 | . 043 | . 076 | . 105 | . 048 | . 081 | . 114 |
| 14 | E | . 503 | . 009 | . 098 | . 161 | . 216 | . 112 | . 184 | . 239 |
| 15 | E | . 684 | . 008 | . 174 | . 285 | . 368 | . 189 | . 318 | . 490 |
| 16 | F | . 235 | . 032 | . 031 | . 051 | . 059 | . 035 | ,055 | , 065 |
| 17 | F | . 424 | . 024 | . 064 | . 118 | . 168 | . 074 | . 129 | . 164 |
| 18 | $F$ | . 617 | . 001 | . 125 | . 239 | . 302 | . 132 | . 225 | . 286 |
| 19 | $\underline{G}$ | . 270 | -. 002 | . 034 | . 058 | . 078 | . 033 | . 047 | . 078 |
| 20 | G | . 368 | -. 020 | . 083 | . 141 | . 183 | . 081 | . 134 | . 164 |
| 21 | G | . 592 | -. 022 | . 182 | . 313 | . 413 | . 167 | . 277 | . 346 |
| 22 | H | . 228 | . 013 | . 029 | . 043 | . 054 | . 026 | . 108 | . 059 |
| 23 | H | . 463 | . 008 | . 126 | . 223 | . 322 | . 116 | . 201 | . 284 |
| 24 | H | . 596 | . 010 | . 205 | . 393 | . 454 | . 186 | . 304 | . 383 |
| 25 | 1 | . 248 | . 039 | . 028 | . 048 | . 059 | . 026 | . 048 | . 064 |
| 26 | 1 | . 389 | . 030 | . 083 | . 132 | . 181 | . 078 | . 134 | . 195 |
| 27 | 1 | - | ---- | ---- | - | -- | ---- | ---- | -- |
| 28 | $J$ | . 297 | -. 013 | . 025 | . 045 | . 071 | . 026 | . 051 | . 085 |
| 29 | $J$ | . 443 | -. 013 | . 075 | . 122 | . 165 | . 085 | . 152 | . 217 |

TABLE 4
HEAVE MOTIONS (CONTINUED)

|  |  |  |  | CREST |  |  | TROUGH |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Condition 30 | Configuration J | $\begin{gathered} H_{1 / 3 / b} \\ .734 \end{gathered}$ | $h_{\mathrm{dc} /{ }_{b}}$ $-.018$ | $h / b$ .198 | $\begin{aligned} & h_{1 / 3 / b} \\ & .314 \end{aligned}$ | $\begin{aligned} & h_{1 / 20 / b} \\ & .372 \end{aligned}$ | $h / b$ .206 | $\begin{gathered} h_{1 / 3} / b \\ .327 \end{gathered}$ | $\begin{gathered} h_{1 / 10 / b}^{b} \\ .407 \end{gathered}$ |
| 31 | K | . 229 | . 009 | . 014 | . 026 | . 038 | . 014 | . 055 | . 042 |
| 32 | K | . 444 | . 017 | . 057 | . 106 | . 152 | . 064 | . 111 | . 143 |
| 33 | K | . 694 | . 010 | . 195 | . 298 | . 356 | . 202 | . 325 | . 425 |
| 34 | L | . 248 | . 031 | . 020 | . 036 | . 046 | . 021 | . 034 | . 048 |
| 35 | L | . 392 | . 024 | . 057 | . 221 | . 277 | . 062 | . 109 | . 137 |
| 36 | $L$ | . 750 | . 014 | . 199 | . 297 | . 329 | . 183 | . 294 | . 327 |
| 37 | M | . 267 | -. 001 | . 031 | . 559 | . 081 | . 041 | . 085 | . 139 |
| 38 | M | . 424 | -. 000 | . 096 | . 159 | . 214 | . 115 | . 219 | . 314 |
| 39 | M | . 714 | -. 005 | . 213 | . 335 | . 418 | . 239 | . 398 | . 509 |
| 40 | $N$ | . 284 | . 047 | . 030 | . 052 | . 068 | . 036 | . 069 | . 094 |
| 41 | $N$ | . 464 | . 056 | . 122 | . 195 | . 243 | . 144 | . 263 | .342 |
| 42 | $N$ | . 617 | . 053 | . 185 | . 284 | . 358 | . 212 | . 363 | . 494 |
| 43 | 0 | . 298 | . 083 | . 041 | . 062 | . 075 | . 046 | . 086 | . 121 |
| 44 | 0 | . 454 | . 089 | .111 | . 180 | . 222 | . 128 | . 218 | . 278 |
| 45 | 0 | - | ----- | ---- | ---- | --- | ---- | --- | ---- |
| 46 | P | . 226 | -. 012 | . 029 | . 052 | . 076 | . 026 | . 042 | . 061 |
| 47 | P | . 399 | $-.006$ | . 099 | . 177 | . 243 | . 088 | . 156 | . 209 |
| 48 | $P$ | . 705 | -. 008 | . 229 | . 364 | . 452 | . 205 | . 307 | . 373 |
| 49 | Q | . 238 | . 020 | . 032 | . 053 | . 069 | . 027 | . 046 | . 058 |
| 50 | Q | . 355 | . 021 | . 090 | . 164 | . 228 | . 081 | . 134 | . 185 |
| 51 | Q | . 620 | . 027 | . 206 | . 352 | . 445 | . 187 | . 308 | . 379 |
| 52 | R | . 221 | . 043 | . 032 | . 054 | . 068 | . 029 | . 048 | . 063 |
| 53 | R | .401 | . 060 | . 090 | . 151 | . 187 | . 079 | . 129 | .171 |
| 54 | R | . 602 | . 065 | . 210 | . 347 | . 443 | . 181 | . 277 | . 319 |
| 55 | S | . 321 | . 020 | . 064 | . 108 | . 136 | . 072 | . 127 | . 175 |
| 56 | S | . 390 | . 014 | . 096 | . 155 | . 201 | . 110 | . 192 | . 253 |
| 57 | S | . 659 | . 008 | . 177 | . 294 | . 368 | . 201 | . 336 | . 436 |
| 58 | T | . 289 | . 013 | . 050 | . 081 | . 102 | . 055 | . 092 | . 117 |

TABLE 4
heave motions (CONTINUEC)

| Condition | Configuration | $H_{1 / 3 / 1}$ | ${ }^{h_{d c} /{ }_{b}}$ | CREST |  |  | TROUGH |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | h/b |  | $\mathrm{F}_{1 / 10 / b}$ | h/b | $h_{1 / 3 / b}$ | h1/10/b |
| 59 | T | . 414 | . 012 | . 085 | . 142 | . 182 | . 096 | . 171 | . 250 |
| 60 | T | . 675 | . 018 | . 160 | . 271 | . 340 | . 182 | . 313 | . 250 |
| 61 | $u$ | . 332 | .0:6 | . 044 | . 076 | . 105 | . 046 | . 074 | . 383 |
| 62 | u | . 483 | . 017 | . 081 | . 129 | . 164 | . 086 | . 138 | . 169 |
| 63 | U | . 602 | . 001 | . 136 | . 227 | . 281 | . 142 | 25 | . 168 |
| 64 | v | . 295 | . 029 | . 059 | . 09 | . 26 |  | . 252 | 341 |
| 65 | v | . 485 | . 030 | . 121 | 201 |  | . 064 | . 115 | . 166 |
| 66 | $v$ | . 688 | . 029 | . 182 |  | . 262 | . 133 | . 237 | . 320 |
| 67 | W | . 275 | . 001 | . 040 | . 302 | . 394 | . 204 | . 356 | . 458 |
| 68 | W | . 479 | . 009 | . 095 |  | . 094 | . 042 | . 066 | . 087 |
| 69 | W | . 636 | . 011 |  | . 15 | . 183 | . 103 | . 169 | . 234 |
| 70 | $x$ | . 228 | -. 017 | . 164 | . 279 | . 367 | . 174 | . 283 | . 353 |
| 71 | $x$ |  |  | . 027 | . 044 | . 054 | . 028 | . 047 | . 065 |
| 72 | x | --.-- | ---- | --- |  |  |  | -..- |  |
| 73 | Y | . 278 | . 012 | . 040 | . 059 | 066 |  |  |  |
| 74 | $Y$ | . 460 | . 001 | . 094 | . 156 | . 066 | . 049 | . 087 | . 121 |
| 75 | Y | . 647 | . 009 | . 153 |  | . 208 | . 113 | . 221 | . 343 |
| 76 | $z$ | . 298 | . 024 | 45 |  |  | . 180 | . 324 | . 442 |
| 77 | 2 | . 551 | . 058 | . 106 |  | . 076 | . 055 | . 098 | . 125 |
| 78 | 2 | . 675 | . 047 | 180 |  | . 208 | . 133 | . 252 | . 333 |
| 79 | AA | . 258 | . 048 |  | . 285 | . 356 | . 206 | . 352 | . 460 |
| 80 | AA | . 487 | . 058 | . 037 | . 057 | . 071 | . 045 | . 084 | . 111 |
| 81 | $A A$ | . 666 |  |  | , | . 166 | . 104 | . 191 | . 290 |
| 82 | BB |  | . 067 | . 184 | . 287 | . 355 | . 213 | . 369 | . 478 |
| 83 |  | . 216 | -. 019 | . 022 | . 040 | . 056 | . 020 | . 035 | . 046 |
| 8 | BB | . 487 | -. 012 | . 126 | . 223 | . 299 | . 110 | . 175 | . 225 |
| 84 | BB | . 634 | -. 011 | . 189 | . 312 | . 419 | . 164 | . 253 | . 318 |
| 85 | CC | . 259 | . 014 | . 034 | . 064 | . 101 | . 029 | . 051 |  |
| 86 | CC | . 401 | . 020 | . 092 | . 167 | . 242 | . 082 | . 129 | . 067 |

## TABLE 4

## heave motions (CONTINUED)

| Condition | Configuration | $H_{1 / 3 / b}$ | $h_{\text {dc/b }}$ | CREST |  |  | TROUGH |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | $h / b$ | $h_{1 / 3 / b}$ | $\mathrm{h}_{1 / 10}{ }_{\mathrm{b}}$ | /b | $\mathrm{h}_{1 / 3 / \mathrm{b}}$ | 10 b |
| 87 | CC | . 685 | . 023 | . 227 | . 384 | . 497 | . 192 | . 298 | . 364 |
| 88 | DD | . 222 | . 040 | . 029 | . 050 | . 070 | . 028 | . 046 | . 059 |
| 89 | DD | . 481 | . 056 | . 146 | . 267 | . 343 | . 118 | . 184 | . 221 |
| 90 | DD | . 614 | . 067 | . 202 | . 356 | . 452 | . 174 | . 293 | . 385 |
| 91 | EE | . 269 | -. 006 | . 050 | . 085 | . 112 | . 043 | . 071 | . 092 |
| 92 | EE | . 462 | +. 002 | . 136 | . 246 | . 352 | . 117 | . 193 | . 252 |
| 93 | EE | . 632 | . 000 | . 203 | . 377 | . 436 | . 183 | . 298 | . 382 |
| 94 | FF | . 223 | . 011 | . 039 | . 068 | . 085 | . 033 | . 057 | . 080 |
| 95 | FF | . 365 | . 015 | . 100 | . 188 | . 303 | . 089 | . 156 | . 194 |
| 96 | FF | . 620 | . 024 | . 171 | . 312 | . 478 | . 198 | . 307 | . 370 |
| 97 | GG | . 218 | . 044 | . 035 | . 061 | . 080 | . 029 | . 047 | . 059 |
| 98 | GG | . 355 | . 051 | . 094 | . 161 | . 223 | . 088 | . 144 | . 194 |
| 99 | GG | . 621 | . 059 | . 204 | . 353 | . 453 | . 185 | . 308 | . 353 |
| 100 | HH | . 247 | -. 015 | . 053 | . 083 | . 103 | . 059 | . 101 | . 131 |
| 101 | HH | . 503 | -. 008 | . 125 | . 204 | . 257 | . 145 | . 267 | . 354 |
| 102 | HH | . 616 | -. 009 | . 165 | . 282 | . 367 | . 189 | . 332 | . 450 |
| 103 | 11 | . 225 | . 012 | . 056 | . 089 | . 112 | . 062 | . 108 | . 139 |
| 104 | 11 | . 453 | . 018 | . 197 | . 169 | . 205 | . 121 | . 209 | . 270 |
| 105 | 11 | . 748 | . 019 | . 201 | . 319 | . 403 | . 222 | . 370 | . 447 |
| 106 | JJ | . 288 | . 032 | . 041 | . 069 | . 087 | . 046 | . 077 | . 096 |
| 107 | JJ | . 478 | . 026 | . 091 | . 145 | . 188 | . 097 | . 162 | . 197 |
| 108 | JJ | . 694 | . 030 | . 167 | . 293 | . 403 | . 203 | . 337 | . 041 |
| 109 | KK | . 219 | -. 024 | . 034 | . 059 | . 079 | . 032 | . 055 | . 072 |
| 110 | KK | . 362 | -. 026 | . 089 | . 156 | . 221 | . 081 | . 141 | . 184 |
| 111 | KK | . 634 | -. 024 | . 201 | . 357 | . 467 | . 190 | . 310 | . 392 |
| 112 | LL | . 219 | . 007 | . 024 | . 042 | . 053 | . 023 | . 040 | . 056 |
| 113 | LL | . 380 | . 004 | . 095 | . 166 | . 238 | . 093 | . 166 | . 234 |
| 114 | LL | . 587 | . 007 | . 210 | . 357 | . 441 | . 192 | . 304 | . 377 |

TABLE 4
heave motions (CONTINUED)

| Condition | Configuration | $H_{1 / 3 / b}$ | $h_{d c} /_{b}$ | CREST |  |  | TROUGH |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | h/b | $\mathrm{h}_{2 / 3} / \mathrm{b}$ | h1/10/b | $h / b$ | $\mathrm{h}_{1 / 3} /{ }_{b}$ | $h_{1 / 10 \%}$ |
| 115 | MM | . 228 | . 033 | . 027 | . 047 | . 066 | . 027 | . 441 | . 583 |
| 116 | MM | . 330 | . 028 | . $\mathrm{C75}$ | . 120 | . 162 | . 076 | . 127 | . 168 |
| 117 | MM | ---- | --- | - | - | ---- | ---- | ---- | ---- |
| 118 | NN | . 215 | -. 011 | . 033 | . 056 | . 073 | . 031 | . 051 | . 063 |
| 119 | NN | . 351 | -. 010 | . 085 | . 148 | . 207 | . 079 | . 131 | . 172 |
| 120 | NN | . 698 | -. 009 | . 226 | . 368 | . 461 | . 206 | . 326 | . 422 |
| 121 | 00 | . 236 | -. 002 | . 035 | . 059 | . 075 | . 029 | . 052 | . 075 |
| 122 | 00 | . 420 | -. 003 | . 112 | . 206 | . 318 | . 101 | . 179 | . 254 |
| 123 | 00 | . 634 | . 305 | . 216 | . 342 | . 405 | . 198 | . 298 | . 337 |
| 124 | PP | . 225 | . 018 | . 026 | . 044 | . 052 | . 025 | . 042 | . 057 |
| 125 | PP | ---- | - | ---- | -- | -- | ---- | --- | --- |
| 126 | PP | ---- | ----- | ---- | ---- | ---- | ---- | ---- | ---- |


| STERM |  |  |
| :---: | :---: | :---: |
| $\bar{\eta}_{s}$ | ${ }^{n} s_{1 / 3}$ | ${ }^{7} \mathbf{S}_{2,10}$ |
| 0.51 | 0.95 | 1.53 |
| 0.98 | 2.04 | 3.41 |
| 1.39 | 2.96 | 5.17 |
| 0.73 | 1.43 | 2.53 |
| 1.37 | 2.84 | 4.38 |
| 1.93 | 4.06 | 6.26 |
| 1.20 | 2.25 | 3.31 |
| 1.84 | 3.84 | 5.97 |
| 2.45 | 5.03 | 7.19 |
| 0.52 | 0.96 | 1.81 |
| 1.82 | 4.36 | 16.23 |
| 2.41 | 5.12 | 7.53 |
| 1.15 | 2.45 | 4.08 |
| 1.94 | 4.13 | 5.95 |
| 2.34 | 5.14 | 7.05 |
| 0.91 | 1.80 | 2.77 |
| 1.66 | 3.59 | 5.42 |
| 2.29 | 4.16 | 5.46 |
| ---- | ---- | ---- |
| 0.57 | 1.02 | 1.74 |
| 0.72 | 1.51 | 2.73 |
| 0.45 | 0.78 | 1.25 |



 Configu-
Condition

|  | STERN |  |
| :---: | :---: | :---: |
| $\bar{\eta}_{s}$ | $n_{s_{1 / 3}}$ | $n_{S_{1 / 10}}$ |
| 0.93 | 2.07 | 3.74 |
| 0.95 | 2.11 | 3.69 |
| 0.72 | 1.33 | 2.12 |
| 0.91 | 1.87 | 3.21 |
| $\cdots-\cdots$ | $-\cdots$ | $-\ldots-$ |
| 0.40 | 0.77 | 1.47 |
| 0.86 | 1.96 | 3.79 |
| 1.06 | 2.21 | 3.95 |
| 0.43 | 0.77 | 1.22 |
| 0.95 | 2.18 | 4.06 |
| 1.39 | 2.98 | 5.00 |
| 0.91 | 1.69 | 2.67 |
| 1.13 | 2.26 | 3.68 |
| 1.39 | 3.05 | 5.40 |
| 0.56 | 1.14 | 2.03 |
| 0.97 | 2.00 | 3.20 |
| 1.43 | 2.70 | 4.26 |
| 0.79 | 1.46 | 2.29 |
| 1.01 | 2.20 | 3.81 |
| 1.51 | 3.20 | 5.12 |
| 1.16 | 2.39 | 3.79 |


 ConfiguCondition


\[

\] Condition




 table 5





TABLE 6
fDDED DRAG IN WAVES

| Condition | Configuration | $\frac{v}{\sqrt{r}}$ | H $1 / 3 / \mathrm{b}$ | $\frac{R_{a}}{w b^{3}}$ |
| :---: | :---: | :---: | :---: | :---: |
| 1 | A | 2.0 | . 260 | . 019 |
| 2 | A | 2.0 | . 417 | . 027 |
| 3 | A | 2.0 | . 664 | . 035 |
| 4 | B | 3.0 | . 261 | . 024 |
| 5 | B | 3.0 | . 409 | . 035 |
| 6 | B | 3.0 | . 647 | . 044 |
| 7 | C | 4.0 | . 275 | . 025 |
| 8 | c | 4.0 | . 436 | . 049 |
| 9 | C | 4.0 | . 647 | . 076 |
| 10 | 0 | 2.0 | . 227 | . 009 |
| 11 | D | 2.0 | . 475 | . 026 |
| 12 | 0 | 2.0 | . 684 | . 039 |
| 13 | E | 3.0 | . 311 | . 045 |
| 14 | E | 3.0 | . 503 | . 066 |
| 15 | E | 3.0 | . 684 | . 078 |
| 16 | F | 4.0 | . 235 | . 065 |
| 17 | F | 4.0 | . 424 | . 110 |
| 18 | F | 4.0 | . 617 | . 155 |
| 19 | $G$ | 2.0 | . 270 | . 012 |
| 20 | G | 2.0 | . 368 | . 017 |
| 21 | G | 2.0 | . 592 | . 022 |
| 22 | H | 3.0 | . 228 | . 028 |
| 23 | H | $3.0{ }^{\circ}$ | . 463 | . 058 |
| 24 | H | 3.0 | . 596 | . 060 |
| 25 | 1 | 4.0 | . 248 | . 057 |
| 26 | 1 | 4.0 | . 380 | . 096 |
| 27 | 1 | 4.0 | ---- | -- |
| 28 | J | 2.0 | . 297 | - |
| 29 | J | 2.0 | . 443 | . 013 |

TABLE 6

## ADDED DRAG IN WAVES (CONTINUED)

| Condition | Configuration | $\frac{v}{\sqrt{\tau}}$ | $\mathrm{H}_{1 / 3} /{ }_{b}$ | $\frac{R_{a}}{w b^{3}}$ |
| :---: | :---: | :---: | :---: | :---: |
| 30 | $J$ | 2.0 | . 734 | .018 |
| 31 | K | 3.0 | . 229 | . 026 |
| 32 | K | 3.0 | . 444 | . 057 |
| 33 | K | 3.0 | . 694 | . 068 |
| 34 | L | 4.0 | . 248 | . 055 |
| 35 | L | 4.0 | . 392 | . 084 |
| 36 | $L$ | 4.0 | . 750 | ---- |
| 37 | M | 2.0 | . 267 | . 014 |
| 38 | $M$ | 2.0 | . 424 | . 030 |
| 39 | M | 2.0 | . 714 | . 034 |
| 40 | N | 3.0 | . 284 | . 015 |
| 41 | $N$ | 3.0 | . 464 | . 031 |
| 42 | $N$ | 3.0 | . 617 | . 035 |
| 43 | 0 | 4.0 | . 298 | . 031 |
| 44 | 0 | 4.0 | . 454 | . 055 |
| 45 | 0 | 4.0 | -- | ---- |
| 46 | P | 2.0 | . 226 | . 014 |
| 47 | P | 2.0 | . 399 | . 024 |
| 48 | P | 2.0 | . 705 | . 030 |
| 49 | Q | 3.0 | . 238 | . 019 |
| 50 | Q | 3.0 | . 355 | . 029 |
| 51 | Q | 3.0 | . 620 | . 043 |
| 52 | R | 4.0 | . 221 | . 020 |
| 53 | R | 4.0 | . 401 | . 044 |
| 54 | R | 4.0 | . 602 | . 058 |
| 55 | S | 2.0 | . 321 | . 024 |
| 56 | S | 2.0 | . 390 | . 033 |
| 57 | 5 | 2.0 | . 659 | . 045 |
| 58 | $T$ | 3.0 | . 289 | . 030 |

TABLE 6
AdDED DRAG IN WAVES (CONTINUED)

| Condition | Configuration | $\frac{\mathrm{V}}{\sqrt{L}}$ | $\mathrm{H}_{1 / 3}{ }_{6}$ | $\frac{R_{a}}{w b^{3}}$ |
| :---: | :---: | :---: | :---: | :---: |
| 59 | $T$ | 3.0 | . 414 | . 054 |
| 60 | $T$ | 3.0 | . 675 | . 070 |
| 61 | U | 4.0 | . 332 | . 079 |
| 62 | $u$ | 4.0 | . 483 | . 101 |
| 63 | U | 4.0 | . 602 | . 127 |
| 64 | v | 2.0 | . 295 | . 016 |
| 65 | $v$ | 2.0 | . 485 | . 031 |
| 66 | $v$ | 2.0 | . 688 | . 043 |
| 67 | W | 3.0 | . 275 | . 024 |
| 68 | w | 3.0 | . 479 | . 058 |
| 69 | w | 3.0 | . 636 | . 064 |
| 70 | $x$ | 4.0 | . 228 | . 044 |
| 71 | $x$ | 4.0 | ---- | ---- |
| 72 | $\chi$ | 4.0 | ---- | -- |
| 73 | $Y$ | 1.75 | . 278 | . 021 |
| 74 | $Y$ | 1.76 | . 460 | . 036 |
| 75 | Y | 1.76 | . 647 | . 053 |
| 76 | $z$ | 2.64 | . 298 | . 022 |
| 77 | 2 | 2.64 | . 551 | ---- |
| 78 | z | 2.64 | . 675 | . 051 |
| 79 | AA | 3.53 | . 258 | . 033 |
| 80 | AA | 3.53 | . 487 | . 059 |
| 81 | AA | 3.53 | . 666 | . 097 |
| 82 | BB | 1.76 | . 216 | . 011 |
| 83 | BB | 1.76 | . 487 | . 035 |
| 84 | BB | 1.76 | . 634 | . 036 |
| 85 | CC | 2.64 | . 259 | . 019 |
| 86 | cc | 2.64 | . 401 | . 039 |
| 87 | CC | 2.64 | . 685 | . 061 |

TABLE 6
ADDED DRAG IN WAVES (CONTINUED)

|  |  | $V$ |  | $\mathrm{R}_{\mathrm{a}}$ |
| :---: | :---: | :---: | :---: | :---: |
| Condition | Configuration | $\sqrt{\text { L }}$ | $1 / 3 / b$ | w $b^{3}$ |
| 88 | DD | 3.53 | . 222 | . 014 |
| 89 | DD | 3.53 | . 481 | . 051 |
| 90 | DD | 3.53 | . 614 | . 063 |
| 91 | EE | 2.0 | . 269 | . 014 |
| 92 | EE | 2.0 | . 462 | . 018 |
| 93 | EE | 2.0 | . 632 | -- |
| 94 | FF | 3.0 | . 223 | . 016 |
| 95 | FF | 3.0 | . 365 | . 025 |
| 96 | FF | 3.0 | . 620 | . 038 |
| 97 | GG | 4.0 | . 218 | . 018 |
| 98 | GG | 4.0 | . 355 | . 037 |
| 99 | GG | 4.0 | . $62 i$ | . 063 |
| 100 | HH | 2.0 | . 247 | . 012 |
| 101 | HH | 2.0 | . 503 | . 026 |
| 102 | HH | 2.0 | . 616 | . 030 |
| 103 | 11 | 3.0 | . 225 | . 035 |
| 104 | 11 | 3.0 | . 453 | . 081 |
| 105 | 11 | 3.0 | . 748 | . 103 |
| 106 | JJ | 4.0 | . 288 | . 038 |
| 107 | JJ | 4.0 | . 468 | . 034 |
| 108 | JJ | 4.0 | . 694 | . 093 |
| 109 | KK | 2.0 | . 219 | . 012 |
| 110 | KK | 2.0 | . 362 | . 024 |
| 111 | KK | 2.0 | . 634 | . 027 |
| 112 | LL | 3.0 | . 219 | . 020 |
| 113 | LL | 3.0 | . 380 | . 046 |
| 114 | LL | 3.0 | . 587 | . 060 |
| 115 | NM | 4.0 | . 228 | . 025 |
| 116 | MM | 4.0 | . 330 | . 055 |

TABLE 6
ADDED DRAG IN WAVES (CONTINUED)

| Condition | Configuration | $\frac{v}{\sqrt{\tau}}$ | H 1/3/b | $\frac{R_{a}}{w b^{3}}$ |
| :---: | :---: | :---: | :---: | :---: |
| 117 | MM | 4.0 | ---- | ---- |
| 118 | NN | 1.0 | . 215 | . 012 |
| 119 | NN | 2.0 | . 351 | . 020 |
| 120 | NN | 2.0 | . 698 | . 032 |
| 121 | 00 | 3.0 | . 236 | . 017 |
| 122 | 00 | 3.0 | . 420 | . 033 |
| 123 | 00 | 3.0 | . 634 | . 040 |
| 124 | PP | 4.0 | . 225 | . 650 |
| 125 | PP | 4.0 | ---- | ---- |
| 126 | PP | 4.0 | ---- | ---- |



Figure 1 - Model Lines




Bow View




Figure 5 - Significant Pitch. $B=10^{\circ}, \tau=3^{\circ}$


Figure 5 - Continued


Figure 5 - Continued



Figure 6 - Significant Heave $B=10^{\circ}, \tau=3^{\circ}$



Figure 6 - Continued
$\qquad$ -



Figure 6 - Continued


Figure 7 - Significant Bow, $C G$, and Stern Acceleration $B=10^{\circ}, \tau=3^{\circ}$


Figure 7 - Continued


Figure 7 - Continued


Added Orag, $\left(B=10, \frac{V}{\sqrt{L}}=3, L / b=7\right)$


Figure 8 - Added Wave Resistance $\beta=10^{\circ}, \tau=3^{\circ}$


Figure 9-Significant Pitch $\beta=20^{\circ}, \tau=3^{\circ}$



Figure 9 - Continued


Figure 9 - Continued


Figure 10 - Significant Heave $\beta=20^{\circ}, \tau=3^{\circ}$



Figure 10 - Continued


Figure 10 - Continued


Figure 11 - Significant Bow, $C G$, and Stern Acceleration $B=20^{\circ}, T=3^{\circ}$


Figure 11 - Continued


Figure 11 - Continued




Added Orag, $\left(\beta=20: \frac{V}{\sqrt{L}}=4, L / b=7\right)$

Figure 12 - Added Wave Resistance $\beta=20^{\circ}, t=3^{\circ}$


Figure 13-Significant Pitch $\beta=30^{\circ}, \tau=3^{\circ}$



Figure 13 - Continued


I'igure 13 - Continued



Figure 14 - Significant Heave $\beta=30^{\circ}, \tau=3^{\circ}$


Figure 14 - Continued



Figure 14 - Continued



Figure 15 - Significant Bow, $C G$, and Stern Acceleration $\beta=30^{\circ}$, $\tau=3^{\circ}$


Figure 15 - Continued


Figure 15 - Continued


Figure 16 - Added Wave Resistance $B=30^{\circ}$, $\tau=3^{\circ}$

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[^0]:    *Expressed as fraction of beam

[^1]:    *Negative sign indicates ainkage of CG

